

# Solutions

1. Explain why multiplication and division are considered opposite operations. How does applying the opposite operation help you solve an equation?

If you multiply by a number and then divide by it you end up with the same value you started with.  
We can use this to isolate and then solve for a variable.

2. Describe a situation that can be modelled with each equation.

a)  $7y = 28$

b)  $z + 5 = 18$

a) A number multiplied by 7 equals 28.

b) Smudger has some marbles. He buys 5 more and now has 18. How many did he originally have?

3. Barbara is solving the equation  $k + 19 = 36$ .

a) Barbara realizes that she subtracted the wrong number. What operation did she mean to perform on both sides of the equal sign?

b) Does she have to start her solution over? Explain.

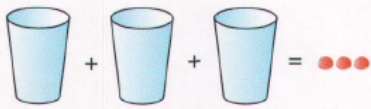
$$k + 19 = 36$$

$$k + 19 - 36 = 36 - 36$$

$$k - 17 = 0$$

- a) She meant to subtract 19 instead of 36 from both sides.
- b) No. She can add 17 to both sides to isolate "k".

4. What equation is modelled by the diagram?



Let  $x =$  a cup

$$x + x + x = 3$$

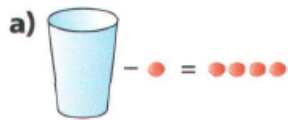
$$3x = 3$$

5. What operation needs to be undone to get the cup by itself in each diagram?

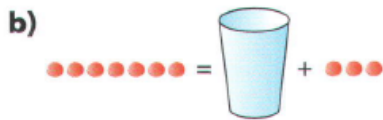


- a) Add 5
- b) Subtract 8

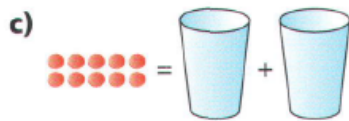
6. Solve the equation modelled by each diagram.



$$\begin{aligned}x - 1 &= 4 \\x - 1 + 1 &= 4 + 1 \\x &= 5\end{aligned}$$



$$\begin{aligned}7 &= x + 3 \\7 - 3 &= x + 3 - 3 \\4 &= x\end{aligned}$$

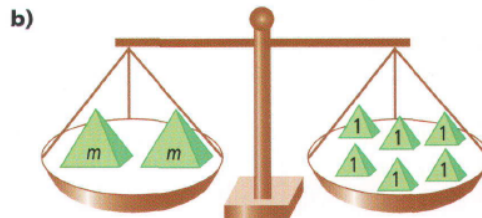


$$\begin{aligned}8 &= x + x \\8 &= \frac{2x}{2} \\4 &= x\end{aligned}$$

8. Find the value of each unknown mass.



$$\begin{aligned}5 &= g + 2 \\5 - 2 &= g + 2 - 2 \\3 &= g\end{aligned}$$



$$\begin{aligned}m + m &= 6 \\2m &= \frac{6}{2} \\m &= 3\end{aligned}$$

9. Oscar gave \$15 toward a school trip. Sandra also gave money toward the trip. Together, they gave \$35.
- Model this situation using cups and counters.
  - What do the cups and counters represent?
  - Write a balanced equation to model this situation.
  - What step would you perform to solve the equation?

Let  $m$  = money Sandra gave

$$15 + m = 35$$

Subtract 15 from both sides to solve the equation.

10. Bill charges \$14 to shovel one driveway. He earned \$112 in February.
- Model this situation using an equation.
  - Solve your equation to find how many driveways Bill shovels in February.

Let  $n$  = # of driveways shovelled

$$\frac{14n}{14} = \frac{112}{14}$$

$$n = 8$$

⇒ Bill shovelled 8 driveways in February.

11. For each expression, write the operation that is performed on the variable. Then, write the opposite operation.

a)  $15 + s$

b)  $p - 100$

c)  $z \div 54$

d)  $17 \times k$

a)  $+15 \rightarrow -15$

b)  $-100 \rightarrow +100$

c)  $\div 54 \rightarrow \times 54$

d)  $\times 17 \rightarrow \div 17$

12. Solve each equation by inspection.

Verify your answer.

a)  $5c = 20$

b)  $16 = 8n$

c)  $5 = w + 5$

d)  $p - 10 = 6$

a)  $4$  [ $5(4) = 20$ ]

b)  $2$  [ $16 = 8(2)$ ]

c)  $0$  [ $5 = 0 + 5$ ]

d)  $16$  [ $16 - 10 = 6$ ]

13. Solve each equation using the opposite operation. Check your answer.

a)  $g + 7 = 13$

b)  $27 = 9m$

c)  $6 = j \div 4$

d)  $q - 4 = 1$

$$\begin{aligned} \text{a) } g + 7 &= 13 \\ g + 7 - 7 &= 13 - 7 \\ g &= 6 \end{aligned}$$

$$\begin{aligned} \text{b) } \frac{27}{9} &= \frac{9m}{9} \\ 3 &= m \end{aligned}$$

$$\begin{aligned} \text{c) } 6 &= j \div 4 \\ 6 \times 4 &= j \div 4 \times 4 \\ 24 &= j \end{aligned}$$

$$\begin{aligned} \text{d) } q - 4 &= 1 \\ q - 4 + 4 &= 1 + 4 \\ q &= 5 \end{aligned}$$

14. Solve each equation. Verify your solution.

a)  $j \div 10 = 12$

b)  $h \div 3 = -6$

c)  $7x = 21$

d)  $18 = f - 2$

$$\begin{aligned} \text{a) } j \div 10 &= 12 \\ j \div 10 \times 10 &= 12 \times 10 \\ j &= 120 \end{aligned}$$

$$\begin{aligned} \text{b) } h \div 3 &= -6 \\ h \div 3 \times 3 &= -6 \times 3 \\ h &= -18 \end{aligned}$$

$$\begin{aligned} \text{c) } \frac{7x}{7} &= \frac{21}{7} \\ x &= 3 \end{aligned}$$

$$\begin{aligned} \text{d) } 18 &= f - 2 \\ 18 + 2 &= f - 2 + 2 \\ 20 &= f \end{aligned}$$

15. Solve each equation. Verify your solution.

a)  $y + 4.9 = 20$       b)  $x + 7.9 = 10.3$

c)  $-2 = y - 8$       d)  $5.7 = b + 3.7$

a)  $y + 4.9 = 20$

$$y + 4.9 - 4.9 = 20 - 4.9$$

$$y = 15.1$$

b)  $x + 7.9 = 10.3$

$$x + 7.9 - 7.9 = 10.3 - 7.9$$

$$x = 2.4$$

c)  $-2 = y - 8$

$$-2 + 8 = y - 8 + 8$$

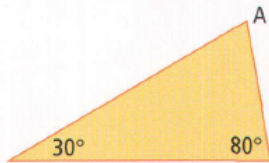
$$6 = y$$

d)  $5.7 = b + 3.7$

$$5.7 - 3.7 = b + 3.7 - 3.7$$

$$2 = b$$

16. The equation  $\angle A + 30^\circ + 80^\circ = 180^\circ$  models the sum of the angles in this triangle. What is the missing angle measure?



$$A + 30 + 80 = 180$$

$$A + 110 = 180$$

$$A + 110 - 110 = 180 - 110$$

$$A = 70^\circ$$

17. A speed skater travels 800 m/min. This can be modelled with the formula  $d = 800t$ .

a) What do the variables represent?

b) How long will it take the skater to travel 5000 m?

a)  $d =$  distance in m  
 $t =$  time in minutes

b)  $d = 800t$

$$\frac{5000}{800} = \frac{800t}{800}$$

$$6.25 = t$$

$\Rightarrow$  It will take 6.25 mins

[or 6 mins 15 secs]