

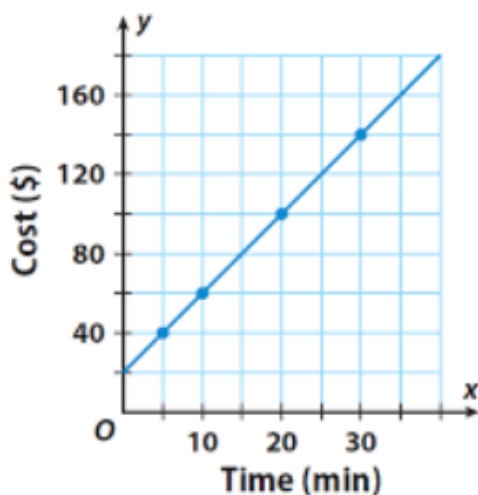
MTH1W Grade 9 Mathematics

3.3 A Closer Look at Rate of Change

Goal(s) - To determine rate of change from a statement, a table of values, and a graph

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Determining Rate of Change from a Graph



Select two points. Beginning with the left most point:

- count the **vertical change** (up or down)
- count the **horizontal change** (count to the right!)
- state as a **ratio** $\frac{\text{vertical change}}{\text{horizontal change}}$

Remember to look at the increments on both scales!!

Determining Rate of Change from a Table of Values

- the **first differences** represent the vertical change on the graph

- the **change of the independent variable** represents the horizontal change on the graph

- state as a **ratio** $\frac{\text{vertical change}}{\text{horizontal change}}$

| x | y | 1 st Differences |
|----|----|-----------------------------|
| -2 | 10 | -3 |
| 0 | 7 | -3 |
| 2 | 4 | -3 |
| 4 | 1 | -3 |
| 6 | -2 | -3 |

$$\text{Vertical change} = -3$$

$$\text{Horizontal change} = 2$$

$$\Rightarrow \text{Ratio (rate of change)} = \frac{-3}{2}$$

Determining Rate of Change from a Statement

- identify the independent and dependent variable

- express as a rate $\frac{y}{x}$

- where possible, express as a **unit rate**

where the change in x is one

A mobile phone plan costs \$110 for two months of service.

$$= 110 \div 2 = \$55 \text{ per month}$$

A cistern is losing water at a rate of 250 L every 5 minutes.

$$= 250 \div 5 = 50 \text{ L/min}$$

The table shows the amount a printing company charges for advertising flyers.

a) Identify the independent and dependent variables.

b) Determine the cost to print 1 flyer.

c) What is the cost to produce 1000 flyers?

d) How many flyers can be produced for \$280?

| Number of Flyers (n) | Cost (c) |
|----------------------|----------|
| 0 | 100 |
| 100 | 120 |
| 200 | 140 |
| 300 | 160 |

initial value (with arrow pointing to 100)

$100 < 0$ and $120 > 20$ (with arrows pointing to 100 and 120)

a) Independent (number of flyers, n)
Dependent (Cost, \$)

$$b) \frac{\text{change in } \$}{\text{change in } n} = \frac{120 - 100}{100 - 0} = \frac{20}{100} = \$0.20 \text{ per flyer}$$

$$c) 1 \text{ flyer} = \$0.20 + \text{initial cost} \\ \Rightarrow 1000 \times \$0.20 + \$100 = \$300$$

$$d) \begin{aligned} 0.20 \times n + 100 &= 280 \\ 0.2n + 100 - 100 &= 280 - 100 \\ \frac{0.2n}{0.2} &= \frac{180}{0.2} \quad n = 900 \text{ flyers} \end{aligned}$$