

Warm Up

Isolate for x in the following equations.

$$y = x + 3$$

$$y - 3 = x$$

$$y = x^2 - 4$$

$$y + 4 = x^2$$

$$\sqrt{y + 4} = x$$

$$y = 2(x - 2)^2$$

$$\frac{y}{2} = \frac{2(x - 2)^2}{2}$$

$$\sqrt{\frac{y}{2}} = x - 2$$

$$2 + \sqrt{\frac{y}{2}} = x$$



Inverse Relations

Lesson objectives

- I know how to find the inverse equation of a function
- I know how to find the domain and range of the inverse from the original function

1.1

Lesson objectives

Teachers' notes

Lesson notes

Nelson Page 46 #s 2ace, 3, 6bdf, 9, 10 & 17

Inverse Function

The reverse of the original function - it undoes what the original function has done.

Example:

If the function is putting on your socks, then your shoes, what would the inverse function be?

Shoes off, then socks off



Inverse Functions - Equation

Example: Write out the steps you would use to evaluate the following function for a given value of x .

$$y = 3\sqrt{x-2} + 4$$

$$\frac{y-4}{3} = \frac{3\sqrt{x-2}}{3}$$

$$\frac{y-4}{3} = \sqrt{x-2}$$

$$\left(\frac{y-4}{3}\right)^2 = x-2$$

$$\left(\frac{y-4}{3}\right)^2 + 2 = x$$

Inverse operations
in reverse order:

subtract 4

divide by 3

square both
sides

add 2



Inverse Functions - Equation

To determine the inverse equation we need to isolate for the independent variable and then switch the variables.

The inverse function is represented by: $f^{-1}(x)$

which is different from: $[f(x)]^{-1}$



Inverse Function - Graphs and Ordered Pairs

In terms of the graph and ordered pairs the reverse of the original is found by simply switching the x and y values.

The graph of the inverse is the reflection of the graph of $y = f(x)$ in the line $y = x$.

$$f(x) = (\text{domain}, \text{range})$$
$$f^{-1}(x) = (\text{range}, \text{domain})$$

They switch!



Example:

Determine the inverse function.

a) $f(x) = \frac{3}{4}x + 2$

$$y = \frac{3}{4}x + 2$$

$$\Rightarrow x = \frac{3}{4}y + 2$$

$$x - 2 = \frac{3}{4}y$$

$$\frac{4(x-2)}{3} = \frac{3y}{3}$$

$$f^{-1}(x) = \frac{4(x-2)}{3}$$

b) $g(x) = -2\sqrt{x+3} - 4$

$$y = -2\sqrt{x+3} - 4$$

$$\Rightarrow x = -2\sqrt{y+3} - 4$$

$$\frac{x+4}{-2} = \frac{-2\sqrt{y+3}}{-2}$$

$$\frac{x+4}{-2} = \sqrt{y+3}$$

$$\left(\frac{x+4}{-2}\right)^2 = y+3$$

$$\left(\frac{x+4}{-2}\right)^2 - 3 = y$$

$$f^{-1}(x) = \left(\frac{x+4}{-2}\right)^2 - 3$$

$$f^{-1}(x) = \frac{(x+4)^2}{4} - 3$$

Example:

Determine the inverse relation for each ordered pair.

a) $\{(-2, 3), (0, 4), (2, 5), (4, 6)\}$

$$\{(3, -2), (4, 0), (5, 2), (6, 4)\}$$

b) $\{(2, 5), (2, -1), (3, 1), (5, 1)\}$

$$\{(5, 2), (-1, 2), (1, 3), (1, 5)\}$$